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### Semester One Examination, 2019

**Question/Answer booklet** 

MATHEMA METHODS UNIT 3 Section One: Calculator-fr	<b>S</b>			
Your name:_				
Teacher nam	e (circle one):	Ai	Friday	Smith
	<b>I for this sectio</b> ore commencing wor	k: five	minutes minutes	
	<b>Juired/recomme</b> by the supervisor swer booklet	ended f	or this sec	tion
-	<b>by the candidate</b> pens (blue/black pr correction fluid/tape	, ·	• •	ling coloured), sharpener ters
Special items:	nil			
Important no	te to candidate	S		

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

### Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available
Section One: Calculator-free	8	8	50	51
Section Two: Calculator-assumed	13	13	100	96

### Instructions to candidates

- 1. The rules for the conduct of examinations are detailed in the school handbook. Sitting this examination implies that you agree to abide by these rules.
- Write your answers in this Question/Answer booklet preferably using a blue/black pen. Do not use erasable or gel pens.
- 3. You must be careful to confine your answer to the specific question asked and to follow any instructions that are specified to a particular question.
- 4. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- 5. It is recommended that you do not use pencil, except in diagrams.
- 6. Supplementary pages for planning/continuing your answers to questions are provided at the end of this Question/Answer booklet. If you use these pages to continue an answer, indicate at the original answer where the answer is continued, i.e. give the page number.
- 7. The Formula sheet is not to be handed in with your Question/Answer booklet.

Markers use only				
Question	Maximum	Mark		
1	6			
2	8			
3	8			
4	5			
5	4			
6	8			
7	5			
8	7			
S1 Total	51			

#### **Section One: Calculator-free**

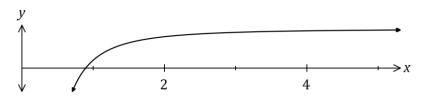
(51 Marks) This section has eight (8) questions. Answer all questions. Write your answers in the spaces provided.

Working time: 50 minutes.

#### **Question 1**

(6 marks)

The curve shown below passes through the point (1, 2) and is such that  $\frac{dy}{dx} = \frac{16}{x^3}$ .



(a) Determine the equation of the curve. (3 marks)

(b) Determine the area of the region enclosed by the curve, the x-axis, the line x = 1 and the line x = 4. (3 marks)

(8 marks)

(1 mark)

### Question 2

A calculator program will generate a single random integer n, where  $3 \le n \le 12$ . The program is run once, and the discrete random variable X is the number of fours or fives obtained.

(a) Explain why *X* is a Bernoulli random variable. (2 marks)

(b) Determine P(X = 1).

(c) Determine the mean and standard deviation of *X*. (2 marks)

The random variable *Y* is the number of fours or fives obtained in three consecutive runs of the program.

(d)	Determine $P(Y \le 1)$ .	(3 marks)
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### Question 3 (8 marks) (a) Determine

(i) 
$$\frac{d}{dx} \frac{\cos(4x)}{x^3}$$
 (2 marks)

(ii) 
$$\frac{d}{dx} \int_{x}^{5} (2\theta + 5)^4 d\theta.$$
 (2 marks)

(b) Find the function A(t) given that A(t) = 
$$\int_{\frac{1}{2}}^{t} \frac{d}{dx} x^2 \sqrt{1 - x^2} dx$$
. (2 marks)

(c) Determine 
$$\int (8x+11)^3 dx$$
. (2 marks)

## Question 4 (5 marks) Let $f(x) = 5x + \frac{k}{2x}$ , x < 0 and k is a constant. The graph of y = f(x) has a stationary point when x = -3.

(a) Determine the value of k.

(2 marks)

(b) Use the second derivative test to determine the nature of the stationary point. (3 marks)

# **Question 5** (4 marks) A random variable *X* has a binomial probability distribution with a mean of 12 and variance of 3.

(a) Determine the value of n and the value of p for this distribution. (2 marks)

(b) Determine the mean and variance of the distribution *Y*, where Y = 5X + 3.3. (2 marks)

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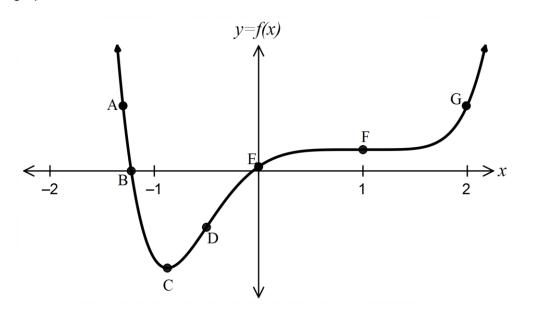
### **Question 6** (8 marks) A vehicle travelling in a straight line has a velocity of 10 ms<sup>-1</sup> as it leaves point Q. The acceleration of the vehicle is given by 3 - 2t ms<sup>-2</sup>, where t is the time in seconds since the

(a)	Determine the velocity of the vehicle when $t = 4$ .	(3 marks)
• •		

(b) Determine how far from Q the vehicle first comes to rest for t > 0. (5 marks)

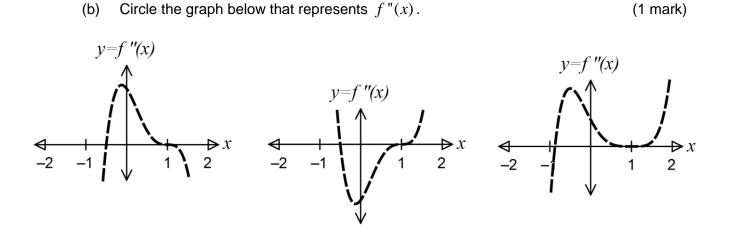
#### **Question 7**

(5 marks) Consider the function y = f(x) shown below. The points, A, B, C, D, E, F and G each lie on the graph.



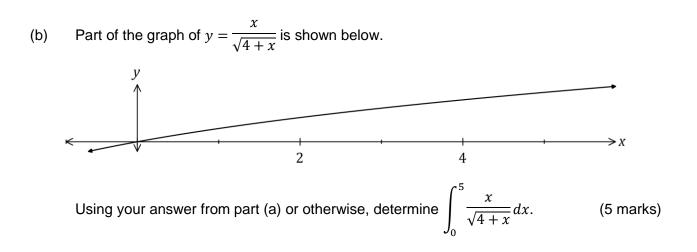
Which point/s labelled on the graph above satisfy the following, (a)

- a point of inflection occurs? (1 mark) (i)
- f'(x) = 0 and  $f''(x) \neq 0$ ? (ii) (1 mark)
- (iii) f is increasing and f''(x) < 0? (1 mark)
- (iv) f(x) > 0 and the function is concave up? (1 mark)





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CALCULATOR-FREE

Supplementary page

Question number: \_\_\_\_\_

Supplementary page

Question number: \_\_\_\_\_